

# Computing Minimalism

Sandiway Fong

Departments of Linguistics and Computer Science

University of Arizona

this work is in part jointly developed with Jason Ginsburg, U. of Aizu, Japan

25th Annual CUNY Conference on Human Sentence Processing. March 14-16, 2012.

# Minimal Computation (MC)

Chomsky (2011)

- language is a computational system:
  - Generative Procedure (GP)
  - Parsing Procedure (PP)
- *we should consider computational efficiency, but...*
- when it comes to Minimal Computation (MC):
  - *conflicts between GP and PP are always resolved in favor of GP*

(12) S' {{that book}, S} = {{that book}, {John, {read, {that, book}}}}

In (12) there are two *copies* of the object {that, book}. S', with the two copies, has the right form for CI (conceptual-intentional) but not of course for SM (sensory-motor)—first because linearization is required and second because the hierarchically less prominent copy is not pronounced. The latter property follows at once from MC: at least the most prominent copy must be pronounced, or there will be no evidence that topicalization took place at all, but computation is reduced if at most one copy is pronounced—massively reduced in nontrivial cases.<sup>8</sup>

# Minimal Computation (MC)

- Chomsky (2011)

also follows from MC. The inadequacy is severe. Anyone who has worked on parsing programs knows that a major difficulty is posed by “filler-gap” problems: given *who* in (10), the problem for parsing/perception is to locate the gap where it receives its interpretation in the argument structure of the sentence, not a trivial matter in general. These problems would largely be obviated if all copies were pronounced, violating MC.

In brief, where there is a conflict between communicative and computational efficiency, the latter seems to win, hands down. It appears that Aristotle’s dictum should be reversed: language is not sound with meaning but meaning with sound, a very different matter. Externalization by the SM system appears to be a secondary property of language.

.. explore idea that the Generative Procedure (GP) and Parsing Procedure (PP) share architecture

*PP can help GP minimize computation*

# What constitutes an implementation?

- Minimalism:
  - (Chomsky 2001) *and later papers*
- Components of the theory:
  1. Recursive Merge (internal/external)
  2. Probe/Goal search (active/inactive)
  3. Agreement (value Case, interpretable/uninterpretable features)
  4. Phases (*limits on search*)

# What constitutes an implementation?

assume, are raising constructions and their exceptional-Case-marking (ECM) counterparts, as shown schematically in (4a), where  $\beta$  is the matrix clause,  $\alpha$  is an infinitival with YP a verbal phrase (the case most relevant here), and P is the probe: T with a raising verb (case (4b)),  $v$  with an ECM transitive verb (case (4c)).<sup>10</sup>

(4) a. [ $\beta$  P [ $\alpha$  [Subj [H YP]]]]

- b. i. there are likely to be awarded several prizes
- ii. several prizes are likely to be awarded
- c. i. we expect there to be awarded several prizes
- ii. we expect several prizes to be awarded

The Case/agreement properties of Subj in (4a), and its overt location, are determined by properties of the matrix probe P, not internally to  $\alpha$ .  $\alpha$  is a TP with defective head  $T_{def}$ , which is unable to determine Case/agreement but has an EPP-feature, overtly manifested in (4c). Raising-ECM parallels give good reason to believe that the EPP-feature is manifested in (4b) as well, by trace of the matrix subject; preference for Merge over (more complex) Move gives a plausible reason for the surface distinction between [Spec,  $T_{def}$ ] in (4b) and in (4c) (see MI). In (4bi) and (4ci), the EPP-feature of  $T_{def}$  is satisfied by Merge of expletive; in (4bii) and (4cii), by raising of the direct object.

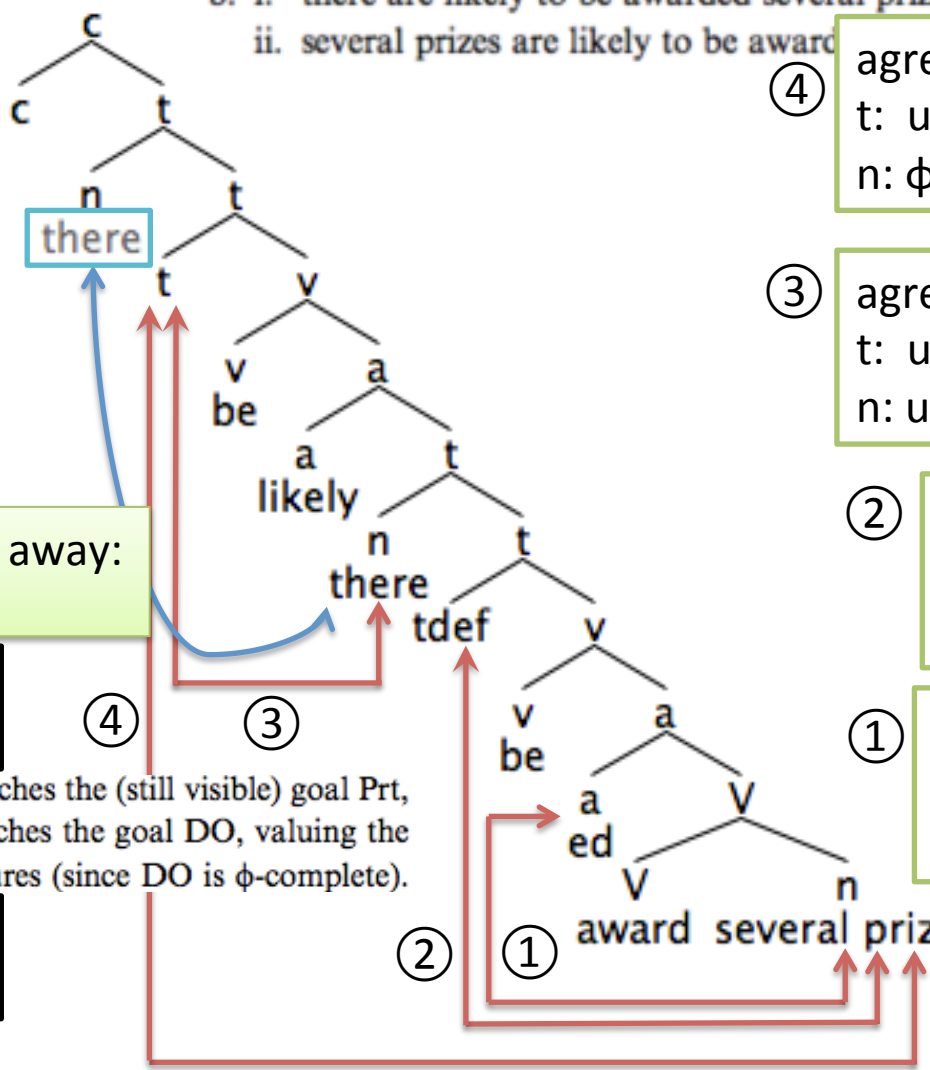
*excerpt from Derivation by Phase*

Grammar formalisms e.g. Stabler (1998), (2011) (Lecomte & Retoré) 2001

# What constitutes an implementation?

1. theta merge V & N
2. merge PRT & V
3. merge v & A
4. merge T & v
5. merge expl & T
6. merge A & Tdef
7. merge v & A
8. merge T & v
9. move to spec-T
10. merge C & T

(4) a. [<sub>β</sub> P [<sub>α</sub> [Subj [H YP]]]]  
 b. i. there are likely to be awarded several prizes  
 ii. several prizes are likely to be awarded



④ agree(t,n)  
 t: uφ, Nominative  
 n: φ, uCase

③ agree(t,n)  
 t: uφ, Nominative  
 n: uφ

② agree(t<sub>def</sub>,n)  
 t<sub>def</sub>: uφ  
 n: φ, uCase

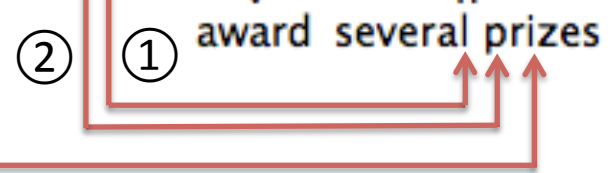
① agree(a,n)  
 -ed: uφ, uCase  
 n: φ, uCase

implementation optimizes this away:  
*uCase can be unified during agree*

\*actually, should need agree(t,a)  
 as well to value Case on PRT

cussed. At the next stage, the probe T/v matches the (still visible) goal PRT, valuing its Case feature; and the probe matches the goal DO, valuing the Case feature of DO as well as its own features (since DO is φ-complete).

one probe, multiple goals:  
 matrix T agrees with 3 goals



# What constitutes an implementation?

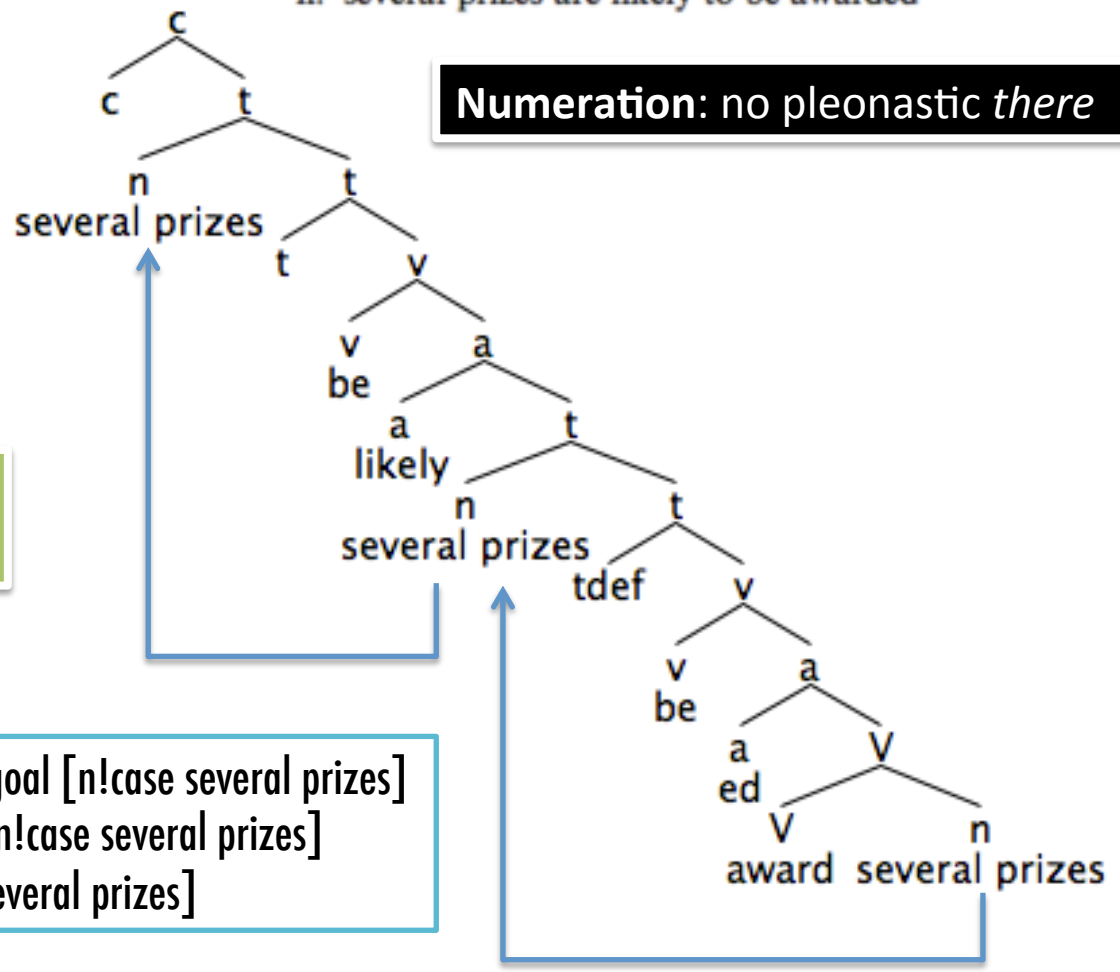
- (4) a. [<sub>β</sub> P [<sub>α</sub> [Subj [H YP]]]]  
 b. i. there are likely to be awarded several prizes  
 ii. several prizes are likely to be awarded

1. theta merge V & N
2. merge PRT & V
3. merge v & A
4. merge T & v
5. move to spec-T
6. merge A & Tdef
7. merge v & A
8. merge T & v
9. move to spec-T
10. merge C & T

same number of Merge steps as before

probe [a!case ed] agrees with goal [n!case several prizes]  
 probe [tdef] agrees with goal [n!case several prizes]  
 probe [t] agrees with goal [n several prizes]

Numeration: no pleonastic *there*





# Computation steps

- Generative Procedure (GP)

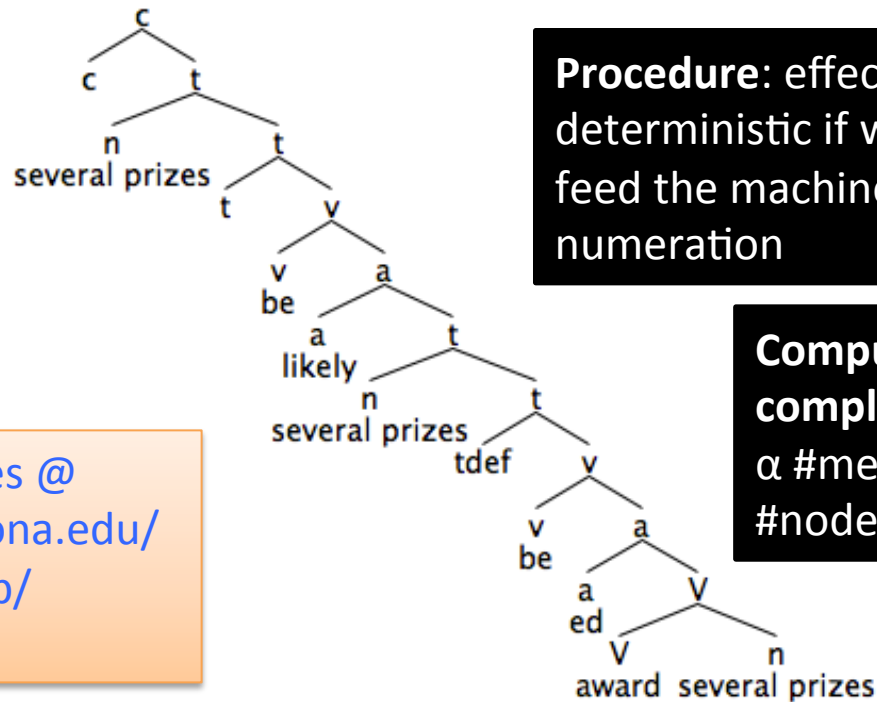


1. theta merge V & N
2. merge PRT & V
3. merge v & A
4. merge T & v
5. move to spec-T
6. merge A & Tdef
7. merge v & A
8. merge T & v
9. move to spec-T
10. merge C & T

step-by-step examples @ <http://dingo.sbs.arizona.edu/~sandiway/mpp/dbyp/examples/>

## Spell-Out

several prizes are likely several prizes to be awarded several prizes



**Procedure:** effectively deterministic if we spoon feed the machine the numeration

**Computational complexity?**  
 $\alpha$  #merge steps +  $\beta$  #nodes probed + ...



# Minimal Computation

- overriding condition of **Minimal Computation (MC)** means design for the **Generative Procedure (GP)**:
  - “*whenever efficiency of design and communication conflicts: design wins*”
- no **Parsing Procedure (PP)** is specified
  - parsing need not be efficient
- **Example:**
  - several prizes are likely ~~several prizes to be awarded several prizes~~

suggest consequences for cognitive architecture. Keeping to the principle of MC, the GP yields forms that are appropriate for semantic interpretation at CI but not for production and perception at sensory-motor (SM), though this SM inadequacy also follows from MC. The inadequacy is severe. Anyone who has worked on parsing programs knows that a major difficulty is posed by “filler-gap” problems: given *who* in (10), the problem for parsing/perception is to locate the gap where it receives its interpretation in the argument structure of the sentence, not a trivial matter in general. These problems would largely be obviated if all copies were pronounced, violating MC.

Chomsky (2011)

# Design Minimalism

## Generative Procedure (GP)

- Design minimalism:
  - good for complexity, but what about data?
- Limits on derivation
  - conservation of syntactic objects (SO)
    - e.g. only copies, can't create indices
- Problem for modules
  - e.g. **Binding theory (BT)** *assuming we still want to have a syntactic BT ...*
    - no Free Indexation
    - no theory-internal levels of representations
    - no Binding Conditions A, B and C

# Growing the implementation

## Binding theory *(joint work with Jason Ginsburg, U. of Aizu, Japan)*

- Idea:

- **doubling constituent** (DC), adapted from Kayne (2002)

- e.g. [he John]  uCase, iφ, theta Merge

[<sub>TP</sub> John thinks [<sub>TP</sub> [he John] [<sub>v</sub> is [<sub>AP</sub> smart [he John]]]]]

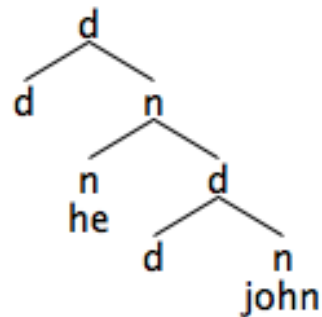
John thinks ~~John~~ he is smart ~~John~~ he

related work:  
Zwart (2002)  
Heinat (2003)

- **Phases**: derive distributional differences between pronouns and anaphors

# John<sub>i</sub> thinks he<sub>i</sub> is smart

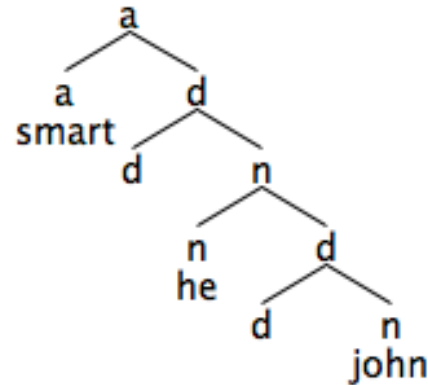
1. merge D & N
2. merge N & D
3. merge D & N
4. theta merge A & N
5. merge v & A
6. merge T & v
7. move to spec-T
8. merge C & T
9. merge V & C
10. merge v\* & V
11. LR move to v\*
12. merge T & v
13. move to spec-T
14. merge C & T



scoreboard	<i>he</i>	<i>John</i>
lacks	theta, Case	theta, Case
licensed		

# John<sub>i</sub> thinks he<sub>i</sub> is smart

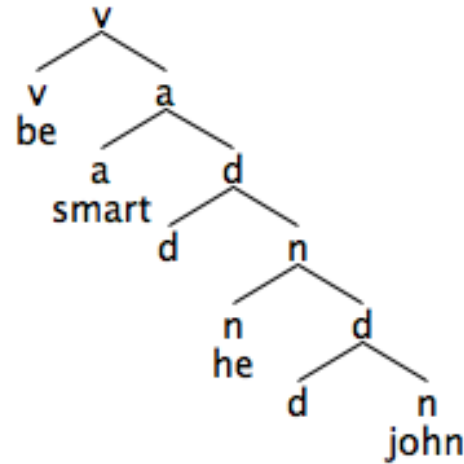
1. merge D & N
2. merge N & D
3. merge D & N
4. theta merge A & N
5. merge v & A
6. merge T & v
7. move to spec-T
8. merge C & T
9. merge V & C
10. merge v\* & V
11. LR move to v\*
12. merge T & v
13. move to spec-T
14. merge C & T



scoreboard	<i>he</i>	<i>John</i>
lacks	Case	theta, Case
licensed	theta	

# John<sub>i</sub> thinks he<sub>i</sub> is smart

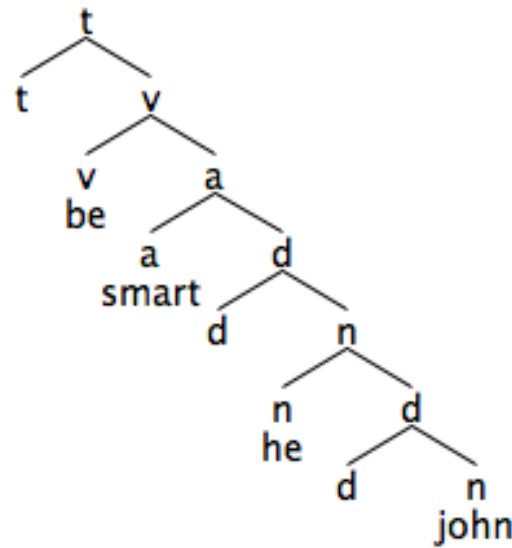
1. merge D & N
2. merge N & D
3. merge D & N
4. theta merge A & N
5. merge v & A
6. merge T & v
7. move to spec-T
8. merge C & T
9. merge V & C
10. merge v\* & V
11. LR move to v\*
12. merge T & v
13. move to spec-T
14. merge C & T



scoreboard	<i>he</i>	<i>John</i>
lacks	Case	theta, Case
licensed	theta	

# John<sub>i</sub> thinks he<sub>i</sub> is smart

1. merge D & N
2. merge N & D
3. merge D & N
4. theta merge A & N
5. merge v & A
6. merge T & v
7. move to spec-T
8. merge C & T
9. merge V & C
10. merge v\* & V
11. LR move to v\*
12. merge T & v
13. move to spec-T
14. merge C & T



Probe [t] agrees with goal [d[d][n[n he][d!case!arg[d][n john]]]]

scoreboard	<i>he</i>	<i>John</i>
lacks		theta, Case
licensed	theta, Case	

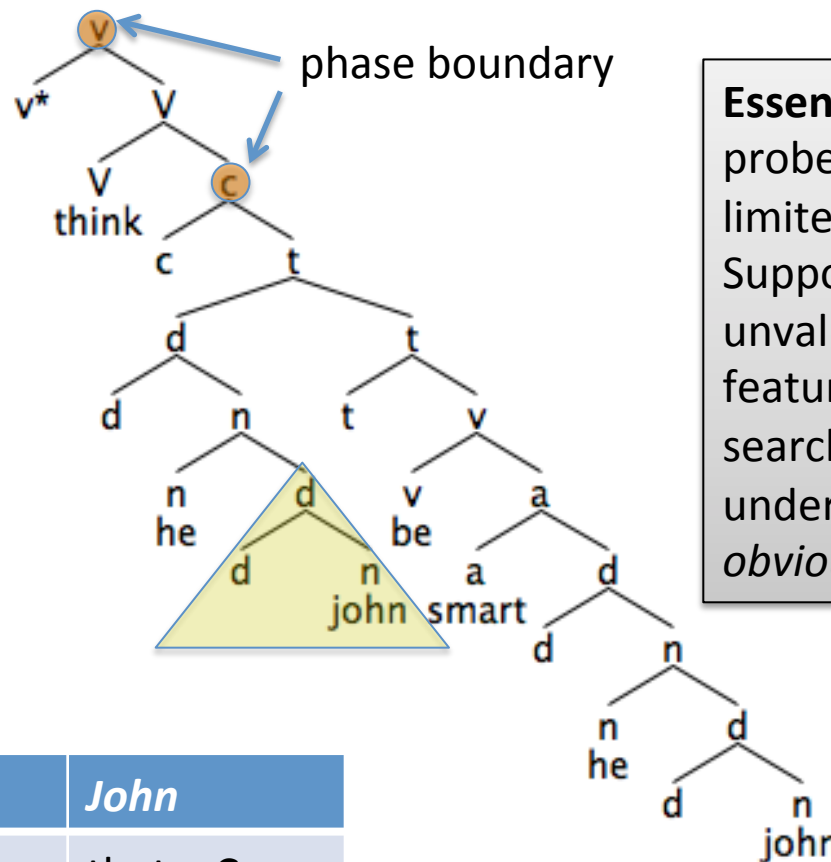






# John<sub>i</sub> thinks he<sub>i</sub> is smart

1. merge D & N
2. merge N & D
3. merge D & N
4. theta merge A & N
5. merge v & A
6. merge T & v
7. move to spec-T
8. merge C & T
9. merge V & C
10. merge v\* & V
11. LR move to v\*
12. merge T & v
13. move to spec-T
14. merge C & T



**Essential idea:**  
 probe-goal search has limited range  
 Suppose r-expr with unvalued uninterpretable feature at the limit of search is allowed to undergo theta Merge ...  
*obviously, timing is critical*

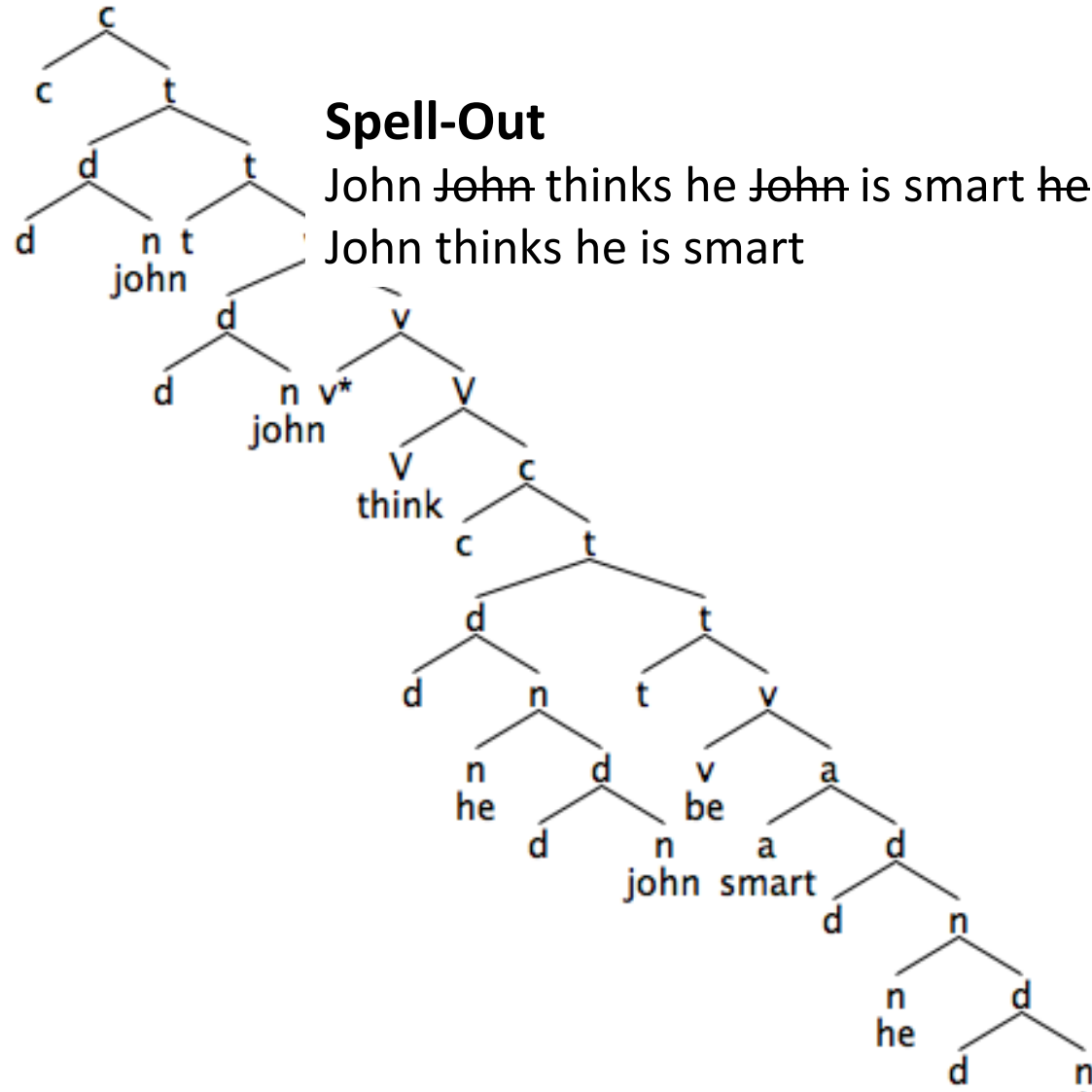
scoreboard	he	John
lacks		theta, Case
licensed	theta, Case	





# John<sub>i</sub> thinks he<sub>i</sub> is smart

1. merge D & N
2. merge N & D
3. merge D & N
4. theta merge A & N
5. merge v & A
6. merge T & v
7. move to spec-T
8. merge C & T
9. merge V & C
10. merge v\* & V
11. LR move to v\*
12. merge T & v
13. move to spec-T
14. merge C & T

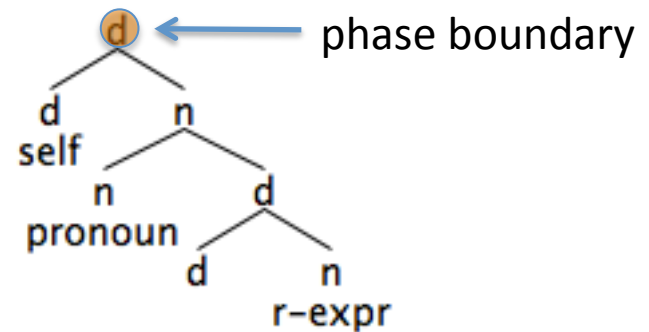


# Data

- Analysis of classic BT data:

- \*John<sub>i</sub> praises him<sub>i</sub>
- John<sub>i</sub> praises himself<sub>i</sub>
- John<sub>i</sub> thinks he<sub>i</sub> is smart
- \*He<sub>i</sub> thinks John<sub>i</sub> is smart
- \*John<sub>i</sub> thinks himself<sub>i</sub> is smart
- \*John<sub>i</sub> thinks that Mary likes himself<sub>i</sub>
- John<sub>i</sub> considers himself<sub>i</sub> to be intelligent
- \*John<sub>i</sub> considers him<sub>i</sub> to be intelligent
- John<sub>i</sub> likes his<sub>i</sub> dog
- \*John<sub>i</sub> likes himself<sub>i</sub>'s dog
- ?\*Hannah<sub>i</sub> found a picture of her<sub>i</sub>
- Hannah<sub>i</sub> found a picture of herself<sub>i</sub>
- ?\*Hannah found Peter<sub>i</sub>'s picture of him<sub>i</sub>
- Hannah found Peter<sub>i</sub>'s picture of himself<sub>i</sub>
- Hannah<sub>i</sub> found Peter's picture of her<sub>i</sub>
- Hannah<sub>i</sub> found Peter's picture of herself<sub>i</sub>
- etc.

assume the DC for anaphors is different to begin with  
[<sub>D</sub> [<sub>D</sub> self][<sub>N</sub> he John]]

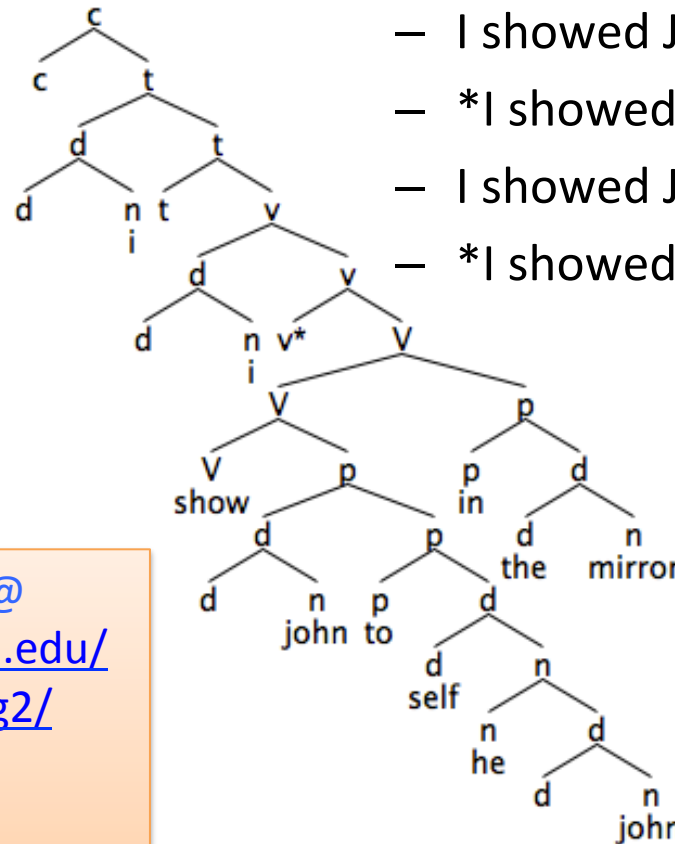


step-by-step examples @  
<http://dingo.sbs.arizona.edu/~sandiway/mpp/binding/examples/>  
also paper



# More Data

1. merge D & N
2. merge N & D
3. merge D & N
4. theta merge P & N
5. LR move to P
6. merge V & P
7. merge D & N
8. theta merge P & N
9. pair-merge v & P
10. merge v\* & V
11. theta merge N & v
12. merge T & v
13. move to spec-T
14. merge C & T



- **double objects**

- I showed John to himself in the mirror
- \*I showed himself to John in the mirror
- I showed John himself in the mirror
- \*I showed himself John in the mirror

step-by-step examples @  
<http://dingo.sbs.arizona.edu/~sandiway/mpp/binding2/examples/>  
 also poster (TCP 2012)  
<http://dingo.sbs.arizona.edu/~sandiway/mpp/TCP2012.pdf>

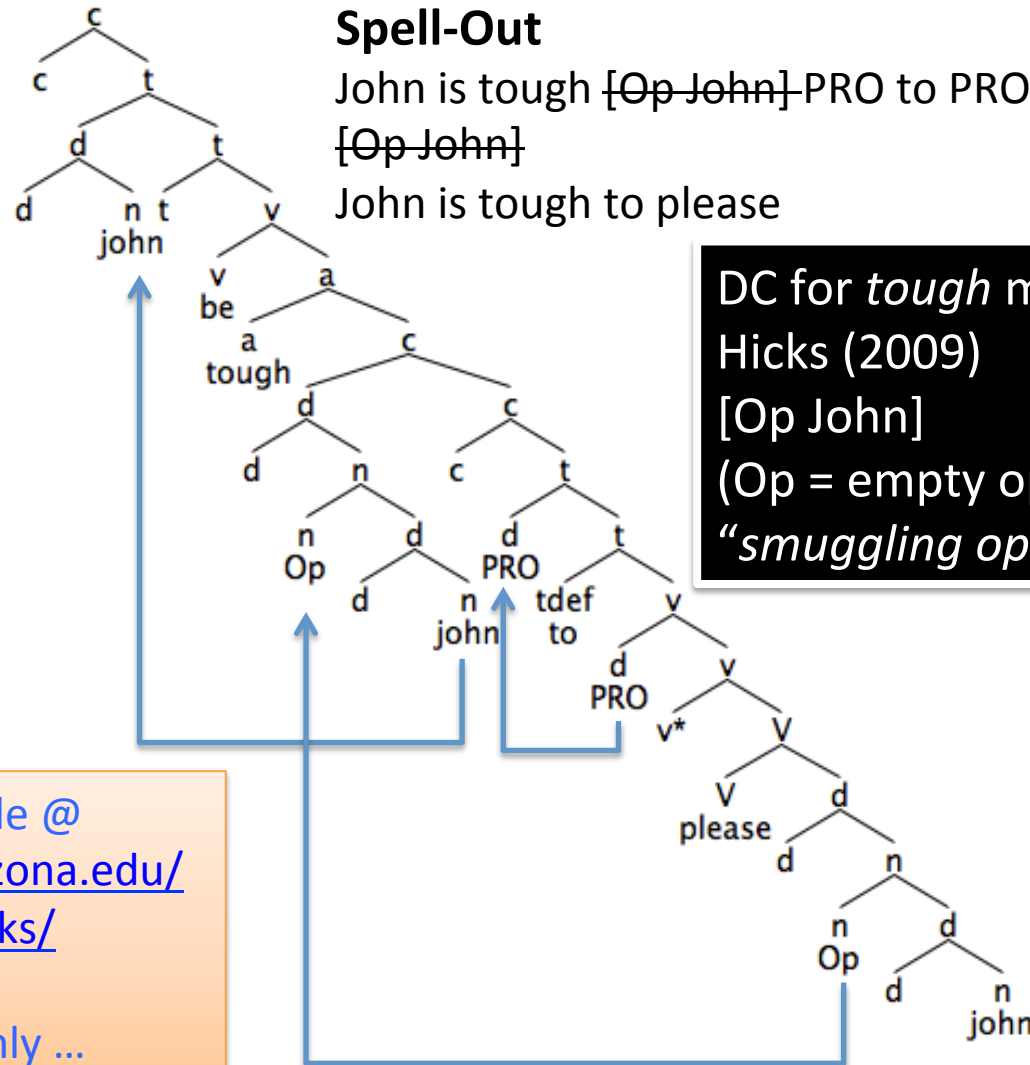
# Even More Data

1. merge D & N
2. theta merge N & D
3. merge D & N
4. theta merge V & N
5. merge v\* & V
6. theta merge N & v
7. merge T & v
8. move to spec-T
9. merge C & T
10. move to spec-C
11. merge A & C
12. merge v & A
13. merge T & v
14. move to spec-T
15. merge C & T

## Spell-Out

John is tough [Op John] PRO to PRO please  
~~[Op John]~~

John is tough to please



DC for *tough* movement  
 Hicks (2009)  
 [Op John]  
 (Op = empty operator)  
 "smuggling operation"

step-by-step example @  
<http://dingo.sbs.arizona.edu/~sandiway/mpp/hicks/examples/>  
 tentative analysis only ...

# Computational Complexity

## Phases

- Long distance:

- **John**<sub>i</sub> thinks that Peter<sub>\*i</sub> thinks that Mary thinks that Bill<sub>\*i</sub> likes **him**<sub>i</sub>

- Cost of locality:

- probe-goal search is local
- iterated movement to the edge of a Phase

coreference possibilities:

[he John] preferred over [he Peter]



# Computational Complexity

## Phases

- Long distance:

- **John**<sub>i</sub> thinks that Peter<sub>\*i</sub> thinks that Mary thinks that Bill<sub>\*i</sub> likes **him**<sub>i</sub>

coreference possibilities:

[he John] preferred over [he Peter]

- Cost of locality:

- probe-goal search is local
  - iterated movement to the edge of a Phase

comes with possible complications:

edge feature management  
order of goals: “tuck in”

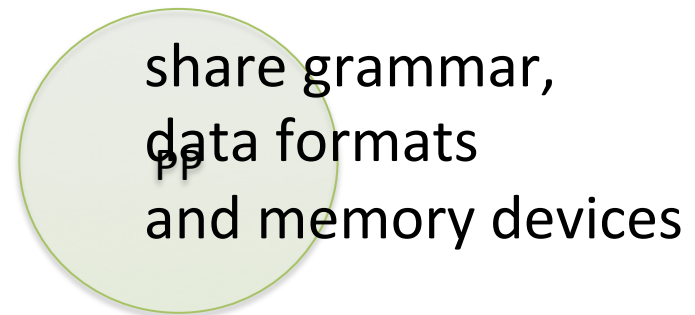
- **Alternate implementation**

*where does this Buffer come from?*

- *eliminate iterated movement of this sort* (smaller trees)
  - use a **Buffer** (for theta Merge)
  - no extra ambiguity
    - **Preference:** external Merge < internal Merge < Buffer

# Generative and Parsing Procedures

- Idea:
  - Generative Procedure (GP) and Parsing Procedure (PP) are not separate devices

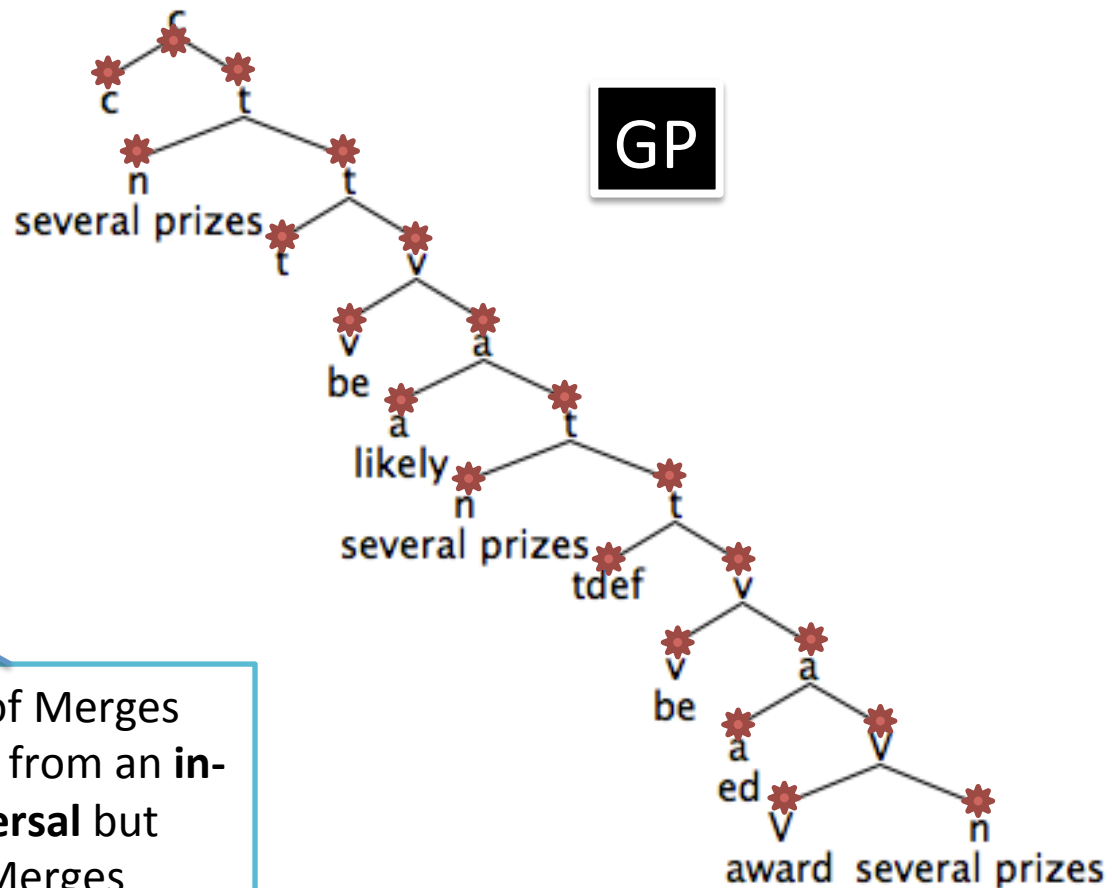


- *but GP has priority over PP* (Minimal Computation)

# Generative and Parsing Procedures

1. theta merge V & N
2. merge PRT & V
3. merge v & A
4. merge T & v
5. move to spec-T
6. merge A & Tdef
7. merge v & A
8. merge T & v
9. move to spec-T
10. merge C & T

sequence of Merges can be had from an **in-order traversal** but reporting Merges on the way back up...





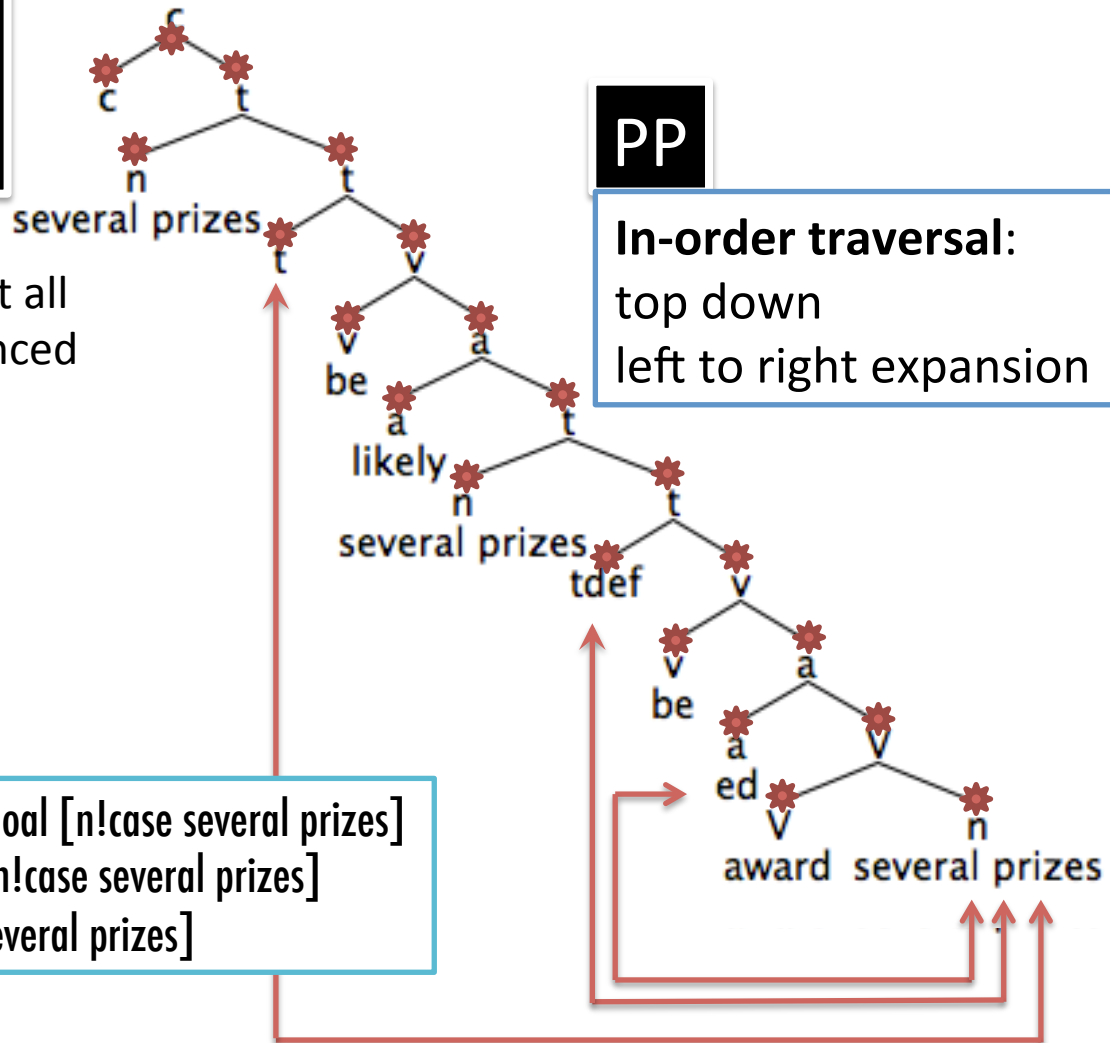
# Generative and Parsing Procedures

Two problems peculiar to parsing that must be dealt with

1. displacement without all copies being pronounced
2. empty heads (t, v and others)

PP

In-order traversal:  
top down  
left to right expansion



probe [a!case ed] agrees with goal [n!case several prizes]  
 probe [tdef] agrees with goal [n!case several prizes]  
 probe [t] agrees with goal [n several prizes]

# Parsing Procedure (PP)

- **Implementation summary**

1. left-to-right, incremental expansion of the covering grammar:

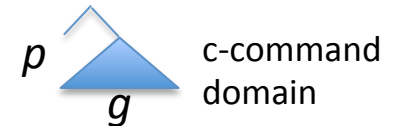
- no need to recode GP

same traversal

GP: report Merges on way back up  
PP: lazy evaluation (*freeze*)

2. probe-goal: GP, PP *nearly the same*

- **timing issues**: active/inactive goals



3. displacement: must put copies in gap positions

- need some memory device: Buffer
- potential ambiguity (fill from input or Buffer)

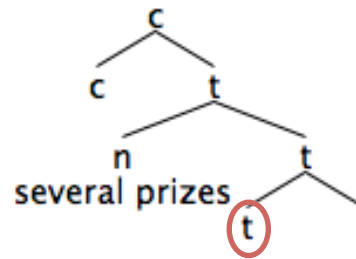
GP: Buffer = internal Merge

4. empty heads: e.g  $T/T_{\text{def}}$ ,  $v/v^*$

- PP (ambiguity), GP (no ambiguity, part of numeration)

# Several prizes are likely to be awarded

```
i [several]
i [several,prizes]
i [several,prizes,be]
i [several,prizes,be,likely]
i [several,prizes,be,likely]
i [several,prizes,be,likely,be]
i [several,prizes,be,likely,be,ed]
i [several,prizes,be,likely,be,ed,award]
i [several,prizes,be,likely,be,ed,award]
f [several,prizes,be,likely,be,ed,award]
```



Buffer [[n|case several prizes]]

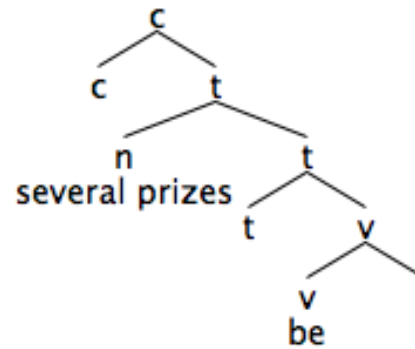
At this point we know there is a copy of *several prizes* downstream  
*but where exactly.. we don't yet have enough information*

## Note:

introduced probe T  
*its c-command domain doesn't exist yet...*  
freeze probe-goal search

# Several prizes are likely to be awarded

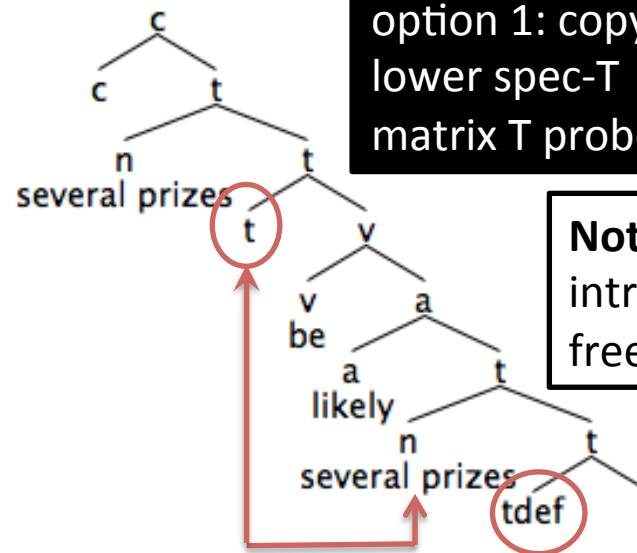
i [several]  
i [several,prizes]  
i [several,prizes,be]  
i [several,prizes,be,likely]  
i [several,prizes,be,likely]  
i [several,prizes,be,likely,be]  
i [several,prizes,be,likely,be,ed]  
i [several,prizes,be,likely,be,ed,award]  
i [several,prizes,be,likely,be,ed,award]  
f [several,prizes,be,likely,be,ed,award]



Buffer [[n!case several prizes]]

# Several prizes are likely to be awarded

```
i [several]
i [several,prizes]
i [several,prizes,be]
i [several,prizes,be,likely]
i [several,prizes,be,likely]
i [several,prizes,be,likely,be]
i [several,prizes,be,likely,be,ed]
i [several,prizes,be,likely,be,ed,award]
i [several,prizes,be,likely,be,ed,award]
f [several,prizes,be,likely,be,ed,award]
```



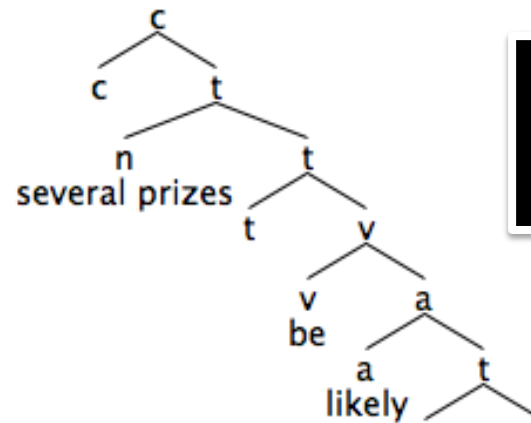
option 1: copy Buffer into open  
lower spec-T  
matrix T probe finds its goal

**Note:**  
introduced probe  $T_{def}$   
freeze probe-goal search

Probe [t] agrees with goal [n several prizes]  
Buffer [[n several prizes]]

# Several prizes are likely to be awarded

i [several]  
i [several,prizes]  
i [several,prizes,be]  
i [several,prizes,be,likely]  
i [several,prizes,be,likely]  
i [several,prizes,be,likely,be]  
i [several,prizes,be,likely,be,ed]  
i [several,prizes,be,likely,be,ed,award]  
i [several,prizes,be,likely,be,ed,award]  
f [several,prizes,be,likely,be,ed,award]

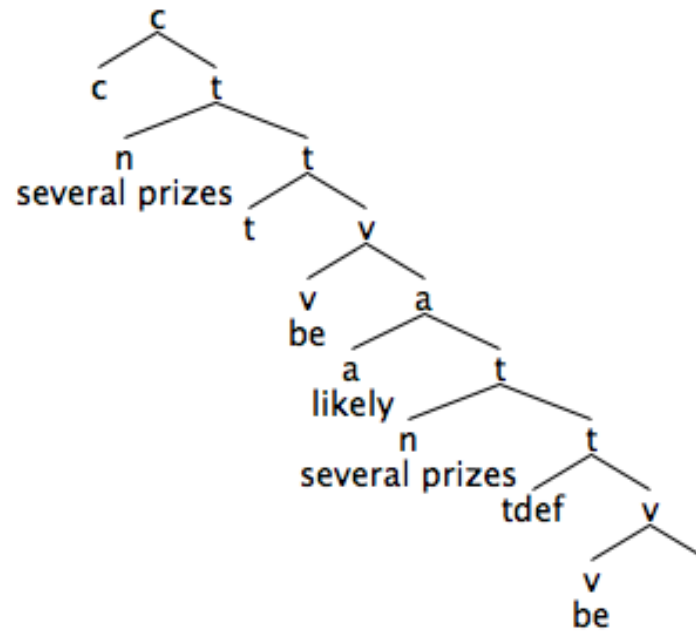


**alternate choice:**  
don't drop *several prizes*  
into subject position

Buffer [[n!case several prizes]]

# Several prizes are likely to be awarded

i [several]  
i [several,prizes]  
i [several,prizes,be]  
i [several,prizes,be,likely]  
i [several,prizes,be,likely]  
i [several,prizes,be,likely,be]  
i [several,prizes,be,likely,be,ed]  
i [several,prizes,be,likely,be,ed,award]  
i [several,prizes,be,likely,be,ed,award]  
f [several,prizes,be,likely,be,ed,award]

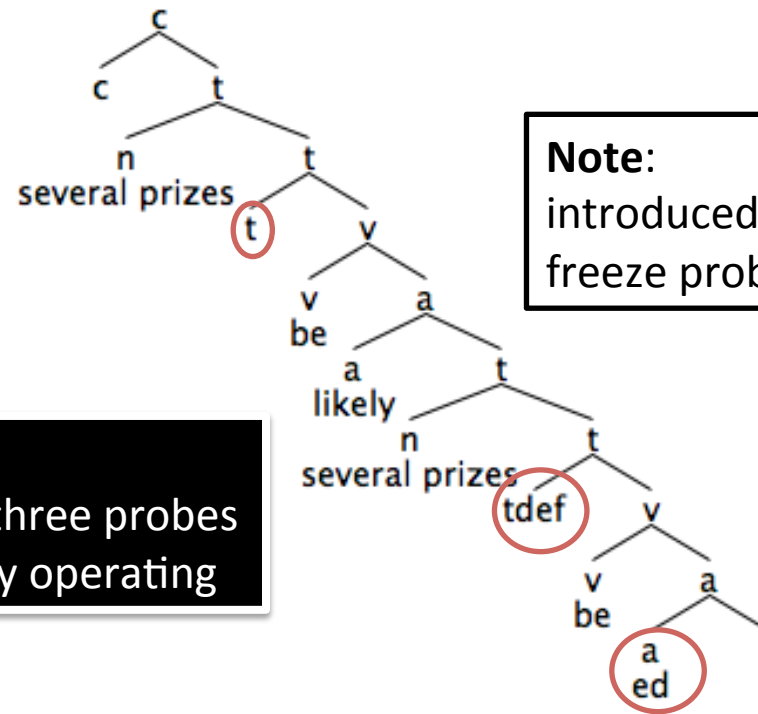


Probe [t] agrees with goal [n several prizes]  
Buffer [[n several prizes]]

# Several prizes are likely to be awarded

i [several]  
i [several,prizes]  
i [several,prizes,be]  
i [several,prizes,be,likely]  
i [several,prizes,be,likely]  
i [several,prizes,be,likely,be]  
i [several,prizes,be,likely,be,ed]  
i [several,prizes,be,likely,be,ed,award]  
i [several,prizes,be,likely,be,ed,award]  
f [several,prizes,be,likely,be,ed,award]

**actually..**  
two out of the three probes  
are concurrently operating



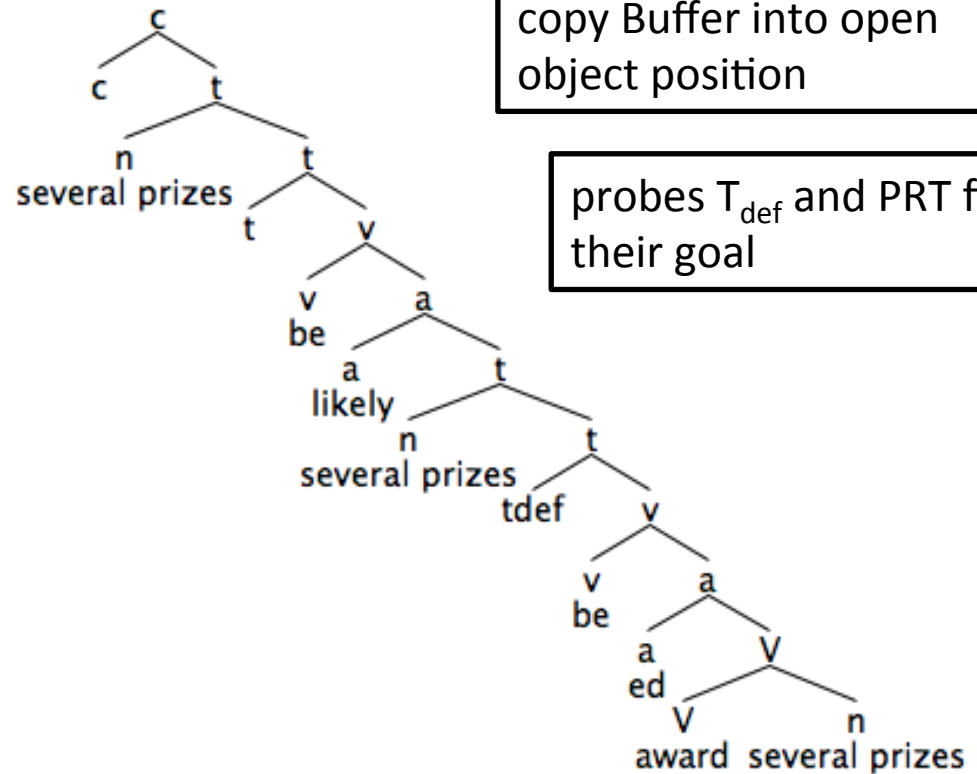
**Note:**  
introduced probe PRT *-ed*  
freeze probe-goal search

Probe [t] agrees with goal [n several prizes]  
Buffer [[n several prizes]]



# Several prizes are likely to be awarded

i [several]  
 i [several,prizes]  
 i [several,prizes,be]  
 i [several,prizes,be,likely]  
 i [several,prizes,be,likely]  
 i [several,prizes,be,likely,be]  
 i [several,prizes,be,likely,be,ed]  
 i [several,prizes,be,likely,be,ed,award]  
 i [several,prizes,be,likely,be,ed,award]  
 f [several,prizes,be,likely,be,ed,award]



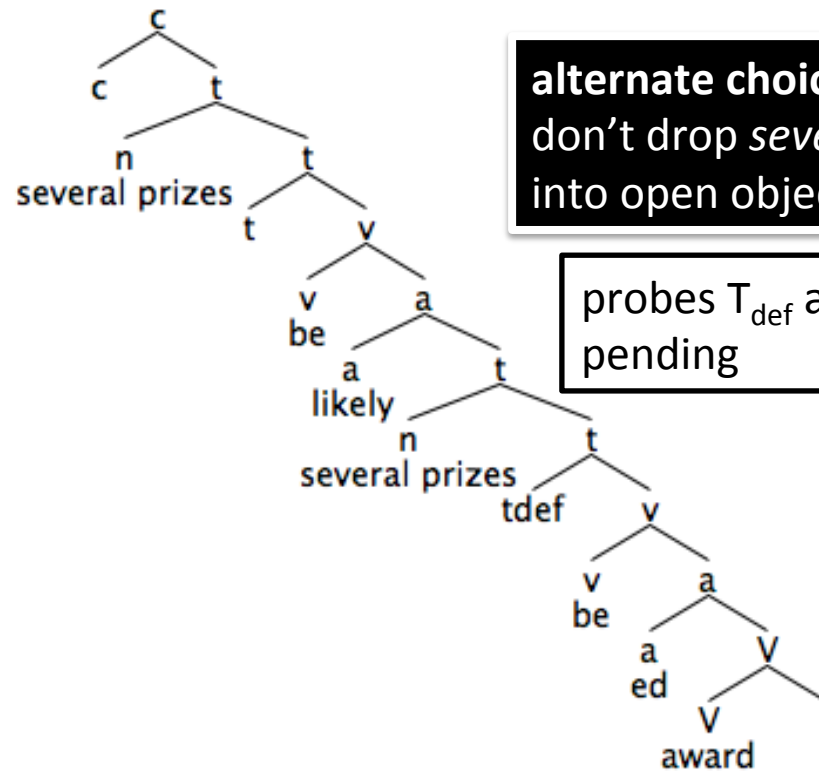
copy Buffer into open object position

probes  $T_{def}$  and PRT find their goal

Probe [t] agrees with goal [n several prizes]  
 Probe [tdef] agrees with goal [n several prizes]  
 Probe [a ed] agrees with goal [n several prizes]

# Several prizes are likely to be awarded

i [several]  
 i [several,prizes]  
 i [several,prizes,be]  
 i [several,prizes,be,likely]  
 i [several,prizes,be,likely]  
 i [several,prizes,be,likely,be]  
 i [several,prizes,be,likely,be,ed]  
 i [several,prizes,be,likely,be,ed,award]  
 i [several,prizes,be,likely,be,ed,award]  
 f [several,prizes,be,likely,be,ed,award]



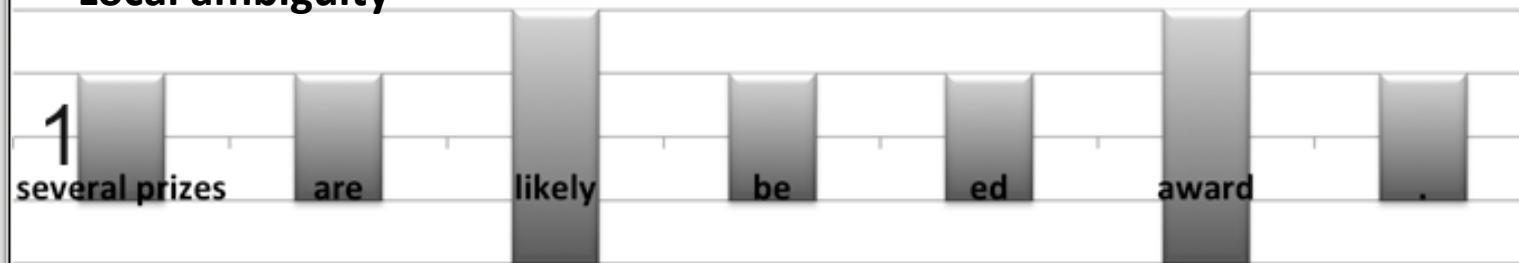
**alternate choice:**  
 don't drop *several prizes*  
 into open object position

probes  $T_{def}$  and PRT still  
 pending

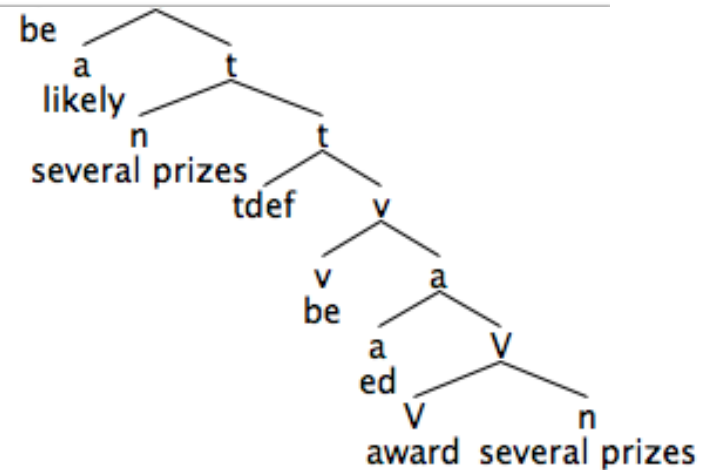
Probe [t] agrees with goal [n several prizes]  
 Buffer [[n several prizes]]

# Several prizes are likely to be awarded

## Local ambiguity



f [several, prizes, be, likely, be, ed, award]

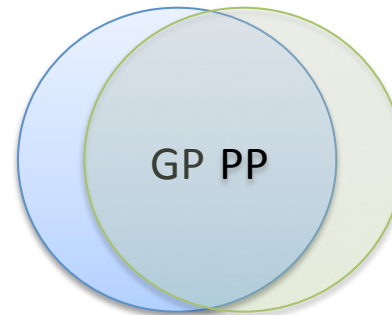


step-by-step examples @  
<http://dingo.sbs.arizona.edu/~sandiway/mpp/cuny2012/examples/>

- Probe [t] agrees with goal [n several prizes]
- Probe [tdef] agrees with goal [n several prizes]
- Probe [a ed] agrees with goal [n several prizes]

# Summary

- **theory:** Chomsky (2001+ ...)
- **implement:** merge, agreement, probe-goal search, phases
- GP and PP share architecture:
  - traverse grammar in same way
  - same probe-goal algorithm
  - MC: we need a memory device to handle displacement
  - PP buffer shared



GP: buffer used in DC analysis for pronoun binding

*improves GP from the standpoint of MC*

# Appendix



# Principles and Parameters Approach

**Parsing: John is too stubborn to talk to Bill**

Generate and  
test:

33 candidate parses  
examined by the parser

*most are eliminated  
early by Case/Theta  
theory sub-system*

