

# LING 364: Introduction to Formal Semantics

Lecture 23

April 11th

# Administrivia

- **Homework 4**
  - graded
  - you should get it back today

# Administrivia

- **this Thursday**
  - computer lab class
  - help with homework 5
  - meet in SS 224

# Today's Topics

- **Homework 4 Review**
- **Finish with**
  - Chapter 6: Quantifiers
  - Quiz 5 (end of class)



# Homework 4 Review

- Prolog definitions common to worlds  $W_1, \dots, W_6$ :
  - horses(Sum) :-
    - findall(X, horse(X), L),
    - sum(L, Sum).
  - sum(L, X+Y) :- pick(X, L, Lp), pick(Y, Lp, \_).
  - sum(L, X+Sum) :- pick(X, L, Lp), **sum**(Lp, Sum).
  - pick(X, [X|L], L).
  - pick(X, [\_|L], Lp) :- pick(X, L, Lp).

# Homework 4 Review

- Questions 1 and 2
- Answers to the query

– ?- findall(PL,horses(PL),L), length(L,N).

– w1 → {A,B}

L = [a+b]

N=1

– w2 → {B,C}

L = [b+c]

N=1

– w3 → {A,B,C}

L = [a+b,a+c,b+c,a+(b+c)]

N=4

– w4 → ∅

L = []

N=0

– w5 → {A,B,C,D,E}

L = [a+b,a+c,a+d,a+e,b+c,b+d,b+e,c+d,c+e,d+e,  
a+(b+c),a+(b+d),a+(b+e),a+(c+d),a+(c+e),a+(d+e),  
a+(b+(c+d)),a+(b+(c+e)),a+(b+(d+e)),  
a+(b+(c+(d+e))),a+(c+(d+e)),b+(c+d),  
b+(c+e),b+(d+e),b+(c+(d+e)),c+(d+e)]

– **total: 26**

The number of combinations is as follows, where number = n and number\_chosen = k:

$$\binom{n}{k} = \frac{P_{k,n}}{k!} = \frac{n!}{k!(n-k)!}$$

where:

$$P_{k,n} = \frac{n!}{(n-k)!}$$

– 2 horses =  ${}_5C_2 = 5!/(2!3!) = 10$

– 3 horses =  ${}_5C_3 = 5!/(3!2!) = 10$

4 horses =  ${}_5C_4 = 5!/(4!1!) = 5$

5 horses = 1

# Homework 4 Review

- **Questions 1 and 2**

- **Answers to the query**

- ?- findall(PL,horses(PL),L), length(L,N).

- w6 → {A,B,C,D,E,F}

- L=[a+b,a+c,a+d,a+e,a+f,b+c,b+d,b+e,b+f,c+d,c+e,c+f,d+e,d+f,e+f,

- a+(b+c),a+(b+d),a+(b+e),a+(b+f),a+(c+d),a+(c+e),a+(c+f),a+(d+e),a+(d+f),a+(e+f),

- a+(b+(c+d)),a+(b+(c+e)),a+(b+(c+f)),a+(b+(d+e)),a+(b+(d+f)),a+(b+(e+f)),

- a+(b+(c+(d+e))),a+(b+(c+(d+f))),a+(b+(c+(e+f))),

- a+(b+(c+(d+(e+f))))),

- a+(b+(d+(e+f))),

- a+(c+(d+e)),a+(c+(d+f)),a+(c+(e+f)),

- a+(c+(d+(e+f))),

- a+(d+(e+f)),

- b+(c+d),b+(c+e),b+(c+f),b+(d+e),b+(d+f),b+(e+f),

- b+(c+(d+e)),b+(c+(d+f)),b+(c+(e+f)),

- b+(c+(d+(e+f))),

- b+(d+(e+f)),

- c+(d+e),c+(d+f),c+(e+f),c+(d+(e+f)),d+(e+f)]

$$2 \text{ horses} = {}_6C_2 = 6!/(2!4!) = 15$$

$$3 \text{ horses} = {}_6C_3 = 6!/(3!3!) = 20$$

$$4 \text{ horses} = {}_6C_4 = 6!/(4!2!) = 15$$

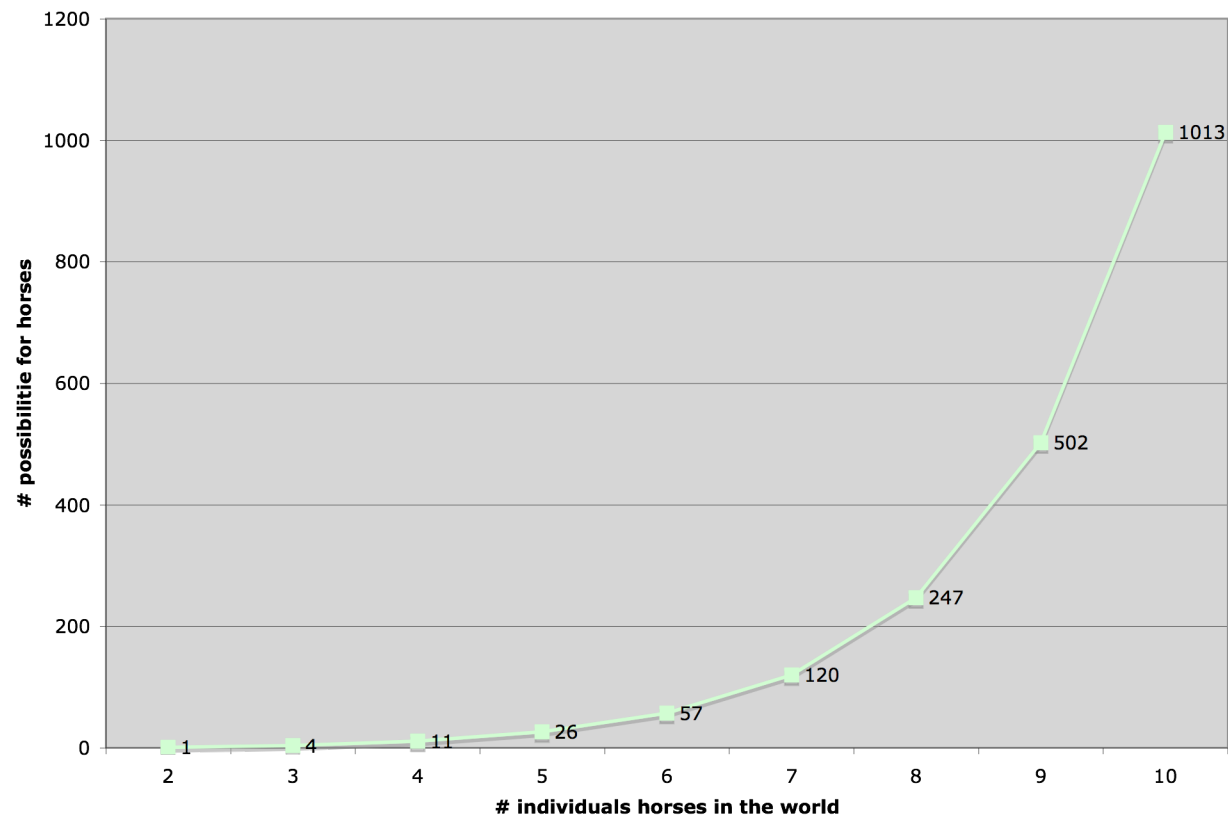
$$5 \text{ horses} = {}_6C_5 = 6!/(5!1!) = 6$$

$$6 \text{ horses} = {}_6C_1 = 1$$

Total: **57**



# Homework 4 Review



# Homework 4 Review

- **Question 3:**
  - What is the Prolog query for “three horses”?
- **Answer**
  - Notice all cases of threes are of pattern/form  $\_+(\ \_+\_ )$  where **each**  $\_$  represents **an individual horse**
    - e.g.  $a+(b+c), a+(b+d), a+(b+e), a+(c+d), a+(c+e), a+(d+e)$
  - **Query (1st attempt)**
    - ?- findall(PL,(horses(PL),PL= $\_+(\ \_+\_ )$ ),L).
  - Example ( $W_5$ )
    - $L=[a+(b+c), a+(b+d), a+(b+e), a+(c+d), a+(c+e), a+(d+e), a+(b+(c+d)), a+(b+(c+e)), a+(b+(d+e)), a+(b+(c+(d+e))), a+(c+(d+e)), b+(c+d), b+(c+e), b+(d+e), b+(c+(d+e)), c+(d+e)]$
    - Total: 16 (**but answer should be 10!**)

# Homework 4 Review

- **Question 3:**
  - What is the Prolog query for “three horses”?
- **Answer**
  - **Query (2nd attempt)**
    - `?- findall(PL,(horses(PL),PL=_+( _+H),\+H=_+_),L), length(L,N).`
  - **Example ( $W_5$ )**
    - `L=[a+(b+c),a+(b+d),a+(b+e),a+(c+d),a+(c+e),a+(d+e),b+(c+d),b+(c+e),b+(d+e),c+(d+e)]`
    - `N=10` (correct)

# Homework 4 Review

- **Question 3:**
  - What is the Prolog query for “three horses”?
- **Another way to deal with the question:**
  - recognize that notation **Horse+Sum** from the given definition:
    - `sum(L,X+Y) :- pick(X,L,Lp), pick(Y,Lp,_).`
    - `sum(L,X+Sum) :- pick(X,L,Lp), sum(Lp,Sum).`
    - is isomorphic to **[Head|Tail]** list notation (here: + is equivalent to |)
- Write a recursive length predicate, call it `len/2`, for **Horse+Sum**
  - `len(_+Sum,N) :- !, len(Sum,M), N is M+1.`
  - `len(_,1).`
- **Query becomes:**
  - `?- findall(PL,(horses(PL),len(PL,3)),L).`

# Homework 4 Review

- **Question 4:**
  - How would you write the query for “the three horses”?
- **Clue** (*given in lecture slides*)
  - `?- findall(X,dog(X),List), length(List,1).`
  - encodes the definite description “the dog”
    - *i.e. query holds (i.e. is true) when dog(X) is true and there is a unique X in a given world*
- *Combine this clue with the answer to Question 3*
- **Resulting Query**
  - `?- findall(PL,(horses(PL),PL=_+( _+H),\+H=_+_ ),L), length(L,1).`
  - Under the assumption that everything is equally salient, query is true for world  $W_3$  only!
  - $L = [a+(b+c)]$
  - Worlds  $W_1, W_2$  and  $W_4$  have too few horses, and worlds  $W_5$  and  $W_6$  have too many.

Back to Chapter 6

# Negative Polarity Items

- **Negative Polarity Items (NPIs)**
- **Examples:**
  - ever, any
- **Constrained distribution:**
  - have to be *licensed* in some way
  - grammatical in a “negated environment” or “question”
- **Examples:**
  - (13a) Shelby **won't** **ever** bite you
  - (13b) **Nobody** has **any** money
  - (14a) \*Shelby will **ever** bite you
  - (14b) \*Noah has **any** money
  - \*= ungrammatical
  - (15a) **Does** Shelby **ever** bite?
  - (15b) **Does** Noah have **any** money?

# Negative Polarity Items

- Inside an *if-clause*:
  - (16a) **If** Shelby **ever** bites you, I'll put him up for adoption
  - (16b) **If** Noah has **any** money, he can buy some candy
- Inside an *every-NP*:
  - (17a) **Every** dog which has **ever** bitten a cat feels the admiration of other dogs
  - (17b) **Every** child who has **any** money is likely to waste it on candy
- Not inside a *some-NP*:
  - (17a) **Some** dog which has **ever** bitten a cat feels the admiration of other dogs
  - (17b) **Some** child who has **any** money is likely to waste it on candy

Not to be confused with free choice (FC) *any* (meaning:  $\forall$ ): *any man can do that*



# Downwards and Upwards Entailment (DE & UE)

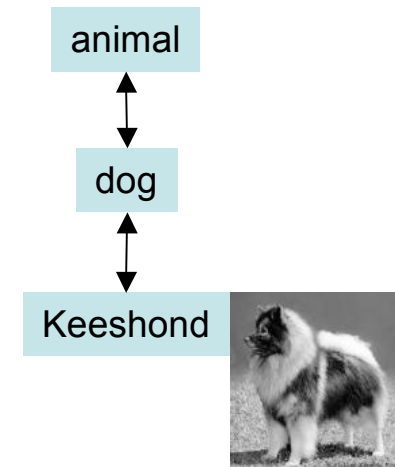
– class  $\Leftrightarrow$  super-class

- **Example:**

- **hyponym**  $\Leftrightarrow$  **hypernym**
- dog  $\Leftrightarrow$  animal
- Keeshond  $\Leftrightarrow$  dog

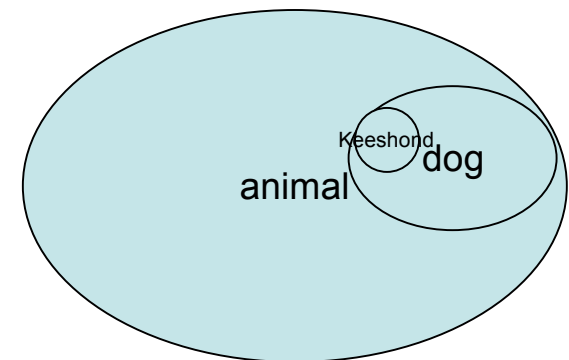
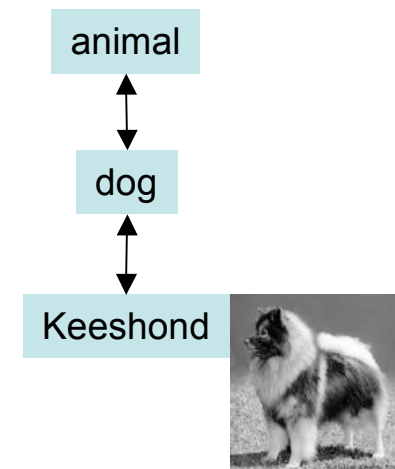
- **Inferencing:**

- non-negative sentence: **upwards**
- (23) I have a dog (entails)
- (23b) I have an animal
- **I have a Keeshond** (invalid inference)
- negative sentence: **downwards**
- (24a) I don't have a dog (entails)
- (24b) I don't have a Keeshond
- **I don't have an animal** (invalid inference)



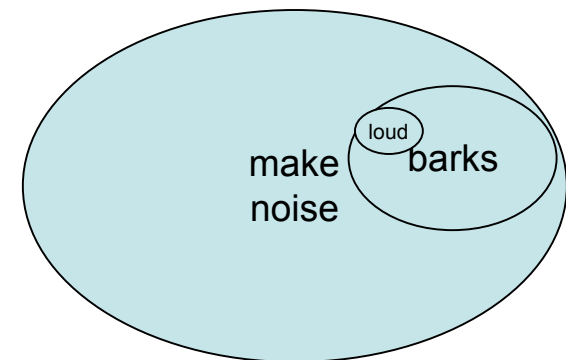
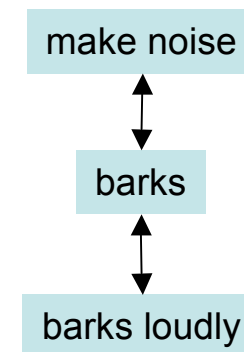
# Downwards and Upwards Entailment (DE & UE)

- Quantifier **every** has semantics
  - $\{X: P_1(X)\} \subseteq \{Y: P_2(Y)\}$
  - e.g. every woman likes ice cream
  - $\{X: \text{woman}(X)\} \subseteq \{Y: \text{likes}(Y, \text{ice\_cream})\}$
- **Every** is **DE** for  $P_1$  and **UE** for  $P_2$
- Examples:
  - (25) a. Every dog barks
  - b. Every Keeshond barks (valid)
  - c. **Every animal barks** (invalid)
    - semantically, “Keeshond” is a sub-property or subset with respect to the set “dog”



# Downwards and Upwards Entailment (DE & UE)

- Quantifier **every** has semantics
  - $\{X: P_1(X)\} \subseteq \{Y: P_2(Y)\}$
  - e.g. every woman likes ice cream
  - $\{X: \text{woman}(X)\} \subseteq \{Y: \text{likes}(Y, \text{ice\_cream})\}$
- **Every** is DE for  $P_1$  and **UE** for  $P_2$
- Examples:
  - (25) a. Every dog barks
  - d. **Every dog barks loudly** (invalid)
  - c. Every dog makes noise (valid)
    - semantically, “barks loudly” is a subset with respect to the set “barks”, which (in turn) is a subset of the set “makes noise”



# Downwards and Upwards Entailment (DE & UE)

- **Inferencing:**

- non-negative sentence: **UE**
- (23) I have a dog (*entails*)
- (23b) I have an animal
- **I have a Keeshond** (invalid)
- **negative sentence: DE**
- (24a) I don't have a dog (*entails*)
- (24b) I don't have a Keeshond
- **I don't have an animal** (invalid)

- **NPI-Licensing:**

- non-negative sentence: **UE**
- (14a) \*Shelby will **ever** bite you
- (14b) \*Noah has **any** money
- **negative sentence: DE**
- (13a) Shelby **won't ever** bite you
- (13b) **Nobody** has **any** money

Generalization:

NPIs like *ever* and *any* are licensed by DE

# Downwards and Upwards Entailment (DE & UE)

- Inside an *every-NP*:
  - (17a) [**Every** [dog][which has **ever** bitten a cat]] feels the admiration of other dogs
  - (17b) [**Every** [child][who has **any** money]] is likely to waste it on candy
- Explanation:
  - **every** is **DE for  $P_1$**  and UE for  $P_2$
  - $\{X: P_1(X)\} \subseteq \{Y: P_2(Y)\}$
- Inside an *every-NP*:
  - (17a)  $P_1 =$  [dog][which has **ever** bitten a cat]
  - (17b)  $P_1 =$  [child][who has **any** money]

Generalization:  
NPIs like *ever* and *any* are licensed by DE

# Quiz 5

- Question 1: Is **Some** UE or DE for  $P_1$  and  $P_2$ ?
  - Lecture 22 (Homework 5 Question 3)
    - *some*:  $\{X: P_1(X)\} \cap \{Y: P_2(Y)\} \neq \emptyset$
  - Justify your answer using examples of valid/invalid inferences starting from
    - Some dog barks
- Question 2: Is **No** UE or DE for  $P_1$  and  $P_2$ ?
  - Lecture 22 (Homework 5 Question 3)
    - *no*:  $\{X: P_1(X)\} \cap \{Y: P_2(Y)\} = \emptyset$
  - Use
    - No dog barks